Mathematics

Number Sense

At around 48 months of age		At around 60 months of age	
1.0	Children begin to understand numbers and quantities in their everyday environment.	1.0	Children expand their under- standing of numbers and quantities in their everyday environment.
1.1	Recite numbers in order to ten with increasing accuracy.	1.1	Recite numbers in order to twenty with increasing accuracy.
1.2	Begin to recognize and name a few written numerals.	1.2	Recognize and know the name of some written numerals.
1.3	Identify, without counting, the number of objects in a collection of up to three objects (i.e., subitize).	1.3	Identify, without counting, the number of objects in a collection of up to four objects (i.e., subitize).
1.4	Count up to five objects, using one-to-one correspondence (one object for each number word) with increasing accuracy.	1.4	Count up to ten objects, using one-to-one correspondence (one object for each number word) with increasing accuracy.
1.5	Use the number name of the last object counted to answer the question, "How many ?"	1.5	Understand, when counting, that the number name of the last object counted represents the total number of objects in the group (i.e., cardinality).
2.0	Children begin to understand number relationships and operations in their everyday environment.	2.0	Children expand their under- standing of number relationships and operations in their everyday environment.
2.1	Compare visually (with or without counting) two groups of objects that are obviously equal or nonequal and communicate, "more" or "same."	2.1	Compare, by counting or matching, two groups of up to five objects and communicate, "more," "same as," or "fewer" (or "less").
2.2	Understand that adding to (or taking away) one or more objects from a group will increase (or decrease) the number of objects in the group.	2.2	Understand that adding one or taking away one changes the number in a small group of objects by exactly one.

At around 48 months of age		At around 60 months of age	
2.3	Understand that putting two groups of objects together will make a bigger group.	2.3	Understand that putting two groups of objects together will make a bigger group and that a group of objects can be taken apart into smaller groups.
2.4	Solve simple addition and subtrac- tion problems nonverbally (and often verbally) with a very small number of objects (sums up to 4 or 5).	2.4	Solve simple addition and subtrac- tion problems with a small number of objects (sums up to 10), usually by counting.

Algebra and Functions (Classification and Patterning)

At around 48 months of age		At around 60 months of age	
1.0	Children begin to sort and classify objects in their everyday environment.	1.0	Children expand their under- standing of sorting and classifying objects in their everyday environment.
1.1	Sort and classify objects by one attribute into two or more groups, with increasing accuracy.	1.1	Sort and classify objects by one or more attributes, into two or more groups, with increasing accuracy (e.g., may sort first by one attribute and then by another attribute).
2.0	Children begin to recognize simple, repeating patterns.	2.0	Children expand their understanding of simple.
			repeating patterns.
2.1	Begin to identify or recognize a simple repeating pattern.	2.1	Recognize and duplicate simple repeating patterns.

Measurement

At around 48 months of age		At around 60 months of age	
1.0	Children begin to compare and order objects.	1.0	Children expand their under- standing of comparing, ordering, and measuring objects.
1.1	Demonstrate awareness that objects can be compared by length, weight, or capacity, by noting gross differences, using words such as <i>bigger, longer, heavier,</i> or <i>taller,</i> or by placing objects side by side to compare length.	1.1	Compare two objects by length, weight, or capacity directly (e.g., putting objects side by side) or indirectly (e.g., using a third object).
1.2	Order three objects by size.	1.2	Order four or more objects by size.
		1.3	Measure length using multiple duplicates of the same-size concrete units laid end to end.

Geometry

At around 48 months of age		At around 60 months of age		
1.0	Children begin to identify and use common shapes in their everyday environment.	1.0	Children identify and use a variety of shapes in their everyday environment.	
1.1	Identify simple two-dimensional shapes, such as a circle and square.	1.1	Identify, describe, and construct a vari- ety of different shapes, including varia- tions of a circle, triangle, rectangle, square, and other shapes.	
1.2	Use individual shapes to represent different elements of a picture or design.	1.2	Combine different shapes to create a picture or design.	
2.0	Children begin to understand positions in space.	2.0	Children expand their under- standing of positions in space.	
2.1	Identify positions of objects and people in space, such as in/on/ under, up/down, and inside/outside.	2.1	Identify positions of objects and people in space, including in/on/under, up/ down, inside/outside, beside/between, and in front/behind.	

Mathematical Reasoning

At around 48 months of age		At around 60 months of age		
1.0	Children use mathematical thinking to solve problems that arise in their everyday environment.	1.0	Children expand the use of mathematical thinking to solve problems that arise in their everyday environment.	
1.1	Begin to apply simple mathematical strategies to solve problems in their environment.	1.1	Identify and apply a variety of math- ematical strategies to solve problems in their environment.	